

# Braking Formulae for Emergency Braking without Electrical Braking

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## SUMMARY

This report shows how equations were derived to be able to calculate the velocity/distance characteristics obtained during the emergency braking of a winder without the use of dynamic braking.

Example calculations are also included in which the characteristics obtained during an overwind test are derived.

## LIST OF SYMBOLS

$C_1$	=	mass of conveyance 1
$M_2$	=	mass of conveyance 2
$M_1$	=	load in conveyance 1
$M_2$	=	load in conveyance 2
$l$	=	total length of the wind
$l_r$	=	total length of the rope
$m$	=	mass per unit length of rope
$X_0$	=	distance of conveyance 1 from end of wind at the time of the trip
$f$	=	allowance for shaft friction
$T_s$	=	static torque
$T_b$	=	braking torque
$T_d$	=	decelerating torque
$R$	=	radius of drum
$R_b$	=	radius of brake path
$B$	=	braking effort
$\mu$	=	coefficient of friction of brake lining
$I_t$	=	total inertia
$I_d$	=	inertia of drums
$I_c$	=	inertia of clutches
$I_s$	=	inertia of drum shaft

$I_a$	=	inertia of armatures referred to the drum shaft
$I_g$	=	inertia of gears
$I_{sh}$	=	inertia of both sheaves referred to the drum shaft
$I_r$	=	inertia due to net load, two conveyances and two ropes
$\alpha$	=	angular acceleration of drum
$a$	=	linear acceleration of conveyance
$F$	=	braking force
$V_0$	=	velocity at time of trip
$t_1$	=	dynamic braking deactuating time delay
$t_2$	=	time after trip until brake shoe contact
$t_3$	=	time after trip until full braking force applied
$S_1$	=	distance at $t_a = t_1$ calculated from equations for $v \leq t_a \leq t_1$ by setting $t = t_1$
$V_1$	=	velocity at $t_a = t_1$ calculated from equations for $0 \leq t_a \leq t_1$ by setting $t = t_1$
$S_2$	=	distance at $t_a = t_2$ calculated from equations for $t_1 \leq t_a \leq t_2$ by setting $t = t_2 - t_1$
$V_2$	=	velocity at $t_a = t_2$ calculated from equations for $t_1 \leq t_a \leq t_2$ by setting $t = t_2 - t_1$
$S_3$	=	distance at $t_a = t_3$ calculated from equations for $t_2 \leq t_a \leq t_3$ by setting $t = t_3 - t_2$
$V_3$	=	velocity at $t_a = t_3$ calculated from equations for $t_2 \leq t_a \leq t_3$ by setting $t = t_3 - t_2$
$s$	=	distance travelled after trip during time $t_a$
$v$	=	velocity at time $t_a$ after trip

$t_a$	=	actual time after trip
$t$	=	time used in calculations
		for $0 \leq t_a \leq t_1$ $t = t_a$
		for $t_1 \leq t_a \leq t_2$ $t = t_a - t_1$
		for $t_2 \leq t_a \leq t_3$ $t = t_a - t_2$
		for $t_3 \leq t_a$ $t = t_a - t_3$
		$n, \psi, \phi, \epsilon_1, \epsilon_2, \alpha_1, \alpha_2, \alpha_3, \beta_1, \beta_2, \beta_3,$ - all calculated constants

### SUMMARY OF BRAKING FORMULAE FOR EMERGENCY BRAKING WITHOUT DYNAMIC BRAKING

$$\text{Total inertia } I_t = I_d + I_c + I_k + I_a + I_g + I_{sh} + 1$$

$$= \sum \text{all individual inertias}$$

$$n^2 = \frac{2 \cdot m \cdot g \cdot R^2}{I_t}$$

$$\gamma = \frac{\mu \cdot R_b \cdot R}{I_t}$$

$$\psi = [(1 - f)(C_1 + M_1 + Ml) - (1 + f)(C_2 + M_2) - 2.M.X_0] \cdot \frac{g \cdot R^2}{I_t}$$

$$\text{Differential equation: } \frac{d^2s}{dt^2} = -n^2 \cdot s = \psi \cdot B + \phi$$

Where B is the function of time

There are four distinct time periods to consider, each period giving a different value for and a different solution to the differential equations.

1

$$\frac{0 \leq t_a \leq t}{B} = 0$$

$$t = t_a$$

$$v = V_0$$

$$s = V_0 \cdot t$$

2

$$\frac{t_1 \leq t_a \leq t_2}{B} = 0$$

$$t = t_a - t_1$$

$$\alpha_1 = S_1 + \frac{\phi}{n^3}$$

$$B_1 = \frac{V_1}{n}$$

$$s = \alpha_1 \cdot \cosh(n \cdot t) + \beta_1 \cdot \sinh(n \cdot t) - \frac{\phi}{n^3}$$

$$v = \alpha_1 \cdot n \sinh(n \cdot t) + \beta_1 \cdot n \cdot \cosh(n \cdot t)$$

3

$$\frac{t_3 \leq t_a \leq t_1}{B} = \frac{F \cdot t}{t_3 - t_2}$$

$$t = t_a - t_2$$

$$\varepsilon_1 = \frac{\gamma \cdot F}{t_3 - t_2}$$

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$$\alpha_2 = S_2 + \frac{\phi}{n_2}$$

$$\beta_2 = \frac{1}{n} \left( V_2 + \frac{\varepsilon_1}{n^2} \right)$$

$$s = \alpha_2 \cdot \cosh(n \cdot t) + \beta_2 \cdot \sinh(n \cdot t) - \frac{(\varepsilon_1, t + \phi)}{n^2}$$

$$v = \alpha_2 \cdot n \cdot \sinh(n \cdot t) - \beta_2 \cdot n \cdot \cosh(n \cdot t) - \frac{\varepsilon_1}{n^2}$$

4

$$\frac{t_3 \leq t_a}{B}$$

$$= F$$

$$t = t_a - t_3$$

$$\varepsilon_2 = \gamma \cdot B + \phi$$

$$\alpha_3 = S_3 + \frac{\varepsilon_2}{n^2}$$

$$\beta_3 = \frac{V_3}{n}$$

$$s = \alpha_3 \cdot \cosh(n \cdot t) + \beta_3 \cdot \sinh(n \cdot t) - \frac{\varepsilon_2}{n^2}$$

$$v = \alpha_3 \cdot n \cdot \sinh(n \cdot t) - \beta_3 \cdot n \cdot \cosh(n \cdot t)$$

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## DERIVATION OF EQUATIONS

### Description

The condition for which the equations were derived is illustrated in Figure 1. This figure also shows how the various distances are measured in relation to each other.

This derivation assumes that any dynamic braking is made inoperative and that only mechanical braking is used after the trip. The time required for the dynamic braking to trip out is catered for.

Figure 2 shows a typical velocity/distance curve obtained after the hoist has been tripped. The curve can be divided into four areas, each of which requires different treatment.

After the trip has occurred there may be a delay ( $t_1$ ) before the dynamic braking cuts out and this results in the curve in area 1 where the velocity neither increases or de-crases by any appreciable amount.

After the dynamic braking has been removed there will be a period of time ( $t_1$  to  $t_2$ ) in which the brakes are not yet in contact with the drum. This is area 2 in Figure 2 and during this time the hoist will accelerate due to gravity.

From the moment the brakes have made contact with the drum their braking effort will start to increase as the brakes are brought more and more onto the drum. After a period ( $t_2$  to  $t_3$ ) the brakes will be fully applied and maximum braking torque will be available. During the initial application of the brakes the braking torque will be less than the static torque of the system and the conveyance will continue to accelerate. When the braking torque becomes sufficient to overcome the static torque the conveyance will start to decelerate. The application of the brakes takes place in area 3 of Figure 2.

After a time  $t_3$  the brakes will be fully applied and the conveyance will be decelerated until it is brought to rest.

### Differential equation

By referring to Figure 1 it can be seen that the static torque on the drum shaft due to the conveyances, load and rope is given by:

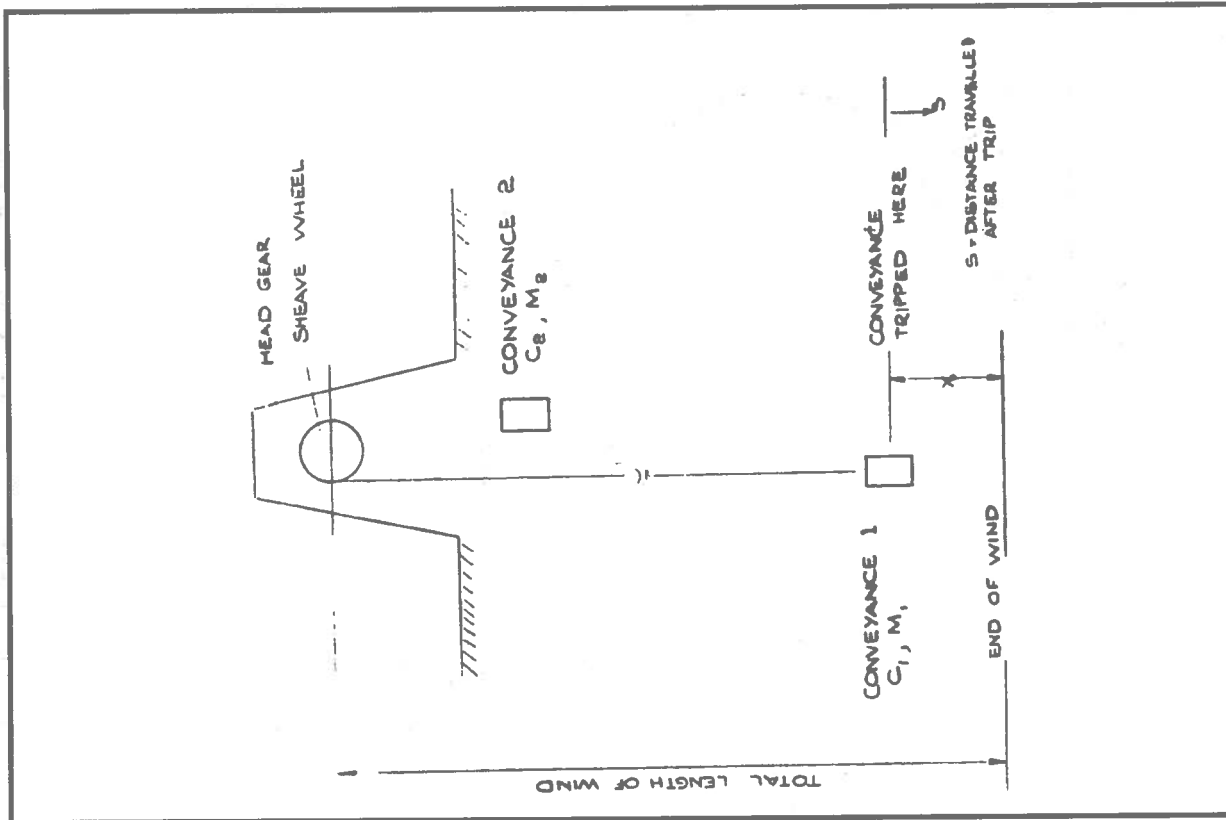


FIGURE 1  
Relation of Distances

$$T_s = [(C_1 - C_2) + (M_1 - M_2) + m[1 - 2(X_o - S)] - \frac{\text{friction}}{\text{allowance}}] \cdot g \cdot R \quad (1)$$

The friction force is mainly due to the rollers in the shaft and windbag. If the friction force is expressed as a percentage of the total suspended weight of the load, conveyances and rope. This will give a static torque of:-

$$T_s = [(C_1 - C_2) + (M_1 - M_2) + m[1 - 2(X_o - S)]] - [(C_1 + C_2) + (M_1 + M_2) + m \cdot l] \cdot f \cdot g \cdot R \quad (2)$$

$$T_s = [(1 - f)(C_1 + M_1 + M \cdot l) - (1 + f)(C_2 + M_2) - 2 \cdot m \cdot X_o + 2 \cdot m \cdot s] \cdot g \cdot R \quad (3)$$

the braking torque is given by:

$$T_b = B \cdot \mu \cdot R_b \quad (4)$$

Where B is dependant upon which area of the curve in Fig 2 the system is operating in. it is because B is different in each area of the curve that four separate sets of equations are needed to fully define the curve.

If the braking torque equals that static torque, the conveyance will continue to move with a constant velocity. Any difference between the braking torque and the static torque will be the torque available to decelerate the conveyance.

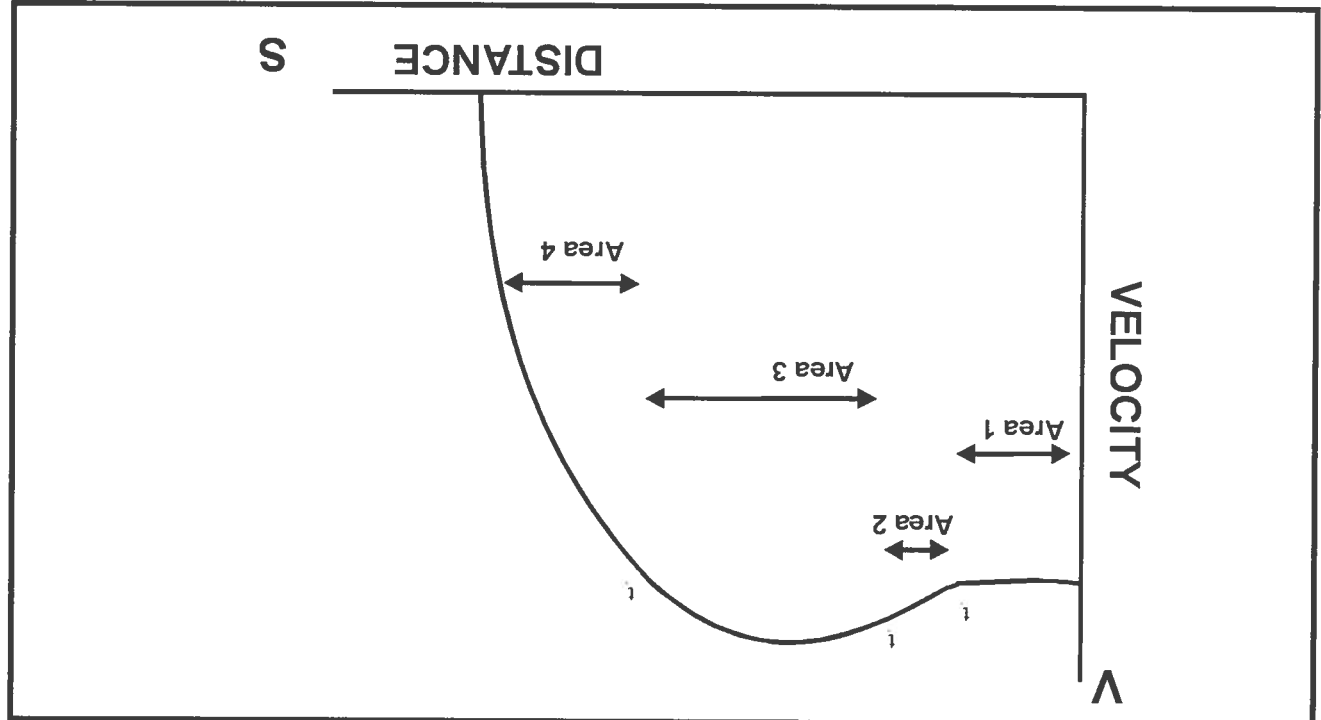
The decelerating torque is given by:

$$t_d = T_b - T_s \quad (5)$$

Having found the decelerating torque, the angular acceleration is given by:

$$\alpha = \frac{T_d}{I_t} = \frac{T_b - T_s}{I_t} \quad (6)$$

FIGURE 2  
Typical Velocity/Distance curve



$$\alpha = \frac{T_a - T_b}{I_t} \quad (7)$$

and the linear acceleration by

$$a = \alpha \cdot R = (T_a - T_b) \cdot \frac{R}{I_t} \quad (8)$$

Substituting equations (3) and (4) into equation (8) we have:

$$a = \{[(1-f)(C_1 + M_1 + m \cdot l) - (1+f)(C_2 + M_2) - 2 \cdot m \cdot X_0 + 2 \cdot m \cdot s] \cdot g \cdot R$$

$$- B \cdot \mu \cdot Rb) \cdot \frac{R}{I_t} \quad (9)$$

$$a = \{[(1-f)(C_1 + M_1 + m \cdot l) - (1+f)(C_2 + M_2) - 2 \cdot m \cdot X_0] \cdot \frac{g \cdot R^2}{I_t} + \frac{2 \cdot m \cdot g \cdot R^2 \cdot s}{I_t} - \frac{B \cdot \mu \cdot R_b \cdot R}{I_t}\} \quad (10)$$

Letting

$$n^2 = \frac{2 \cdot m \cdot g \cdot R^2}{I_t} \quad (11)$$

$$\phi = [(1-f)(C_1 + M_1 + m \cdot l) - (1+f)(C_2 + M_2) - 2 \cdot m \cdot X_0] \cdot \frac{g \cdot R^2}{I_t} \quad (12)$$

$$\psi = - \frac{\mu \cdot Rb \cdot R}{I_t} \quad (13)$$

we have:

$$a = \phi + n^2 \cdot s + \psi \cdot B$$

Now the acceleration  $a = \frac{d^2s}{dt^2}$  and substituting in equation (14) and rearranging we have:

This is a second order differential equation whose general solution is:

$$s = \alpha \cdot \cosh(n \cdot t) + B \cdot \sinh(n \cdot t) + \text{particular integral} \quad (16)$$

The particular integral is dependent upon the area in Fig 2 in which the system is operating.

Having obtained the specific solution to equation (16) the velocity is given by:

$$v = \frac{ds}{dt}$$

### Specific Solutions

The specific solutions are derived for each area as follows:

$$1 \quad 0 \leq t \leq t_a$$

During this period it is assumed that the dynamic braking present cancels out any accelerating torque due to gravity. This gives the following linear motion equations:

$$v = V_0 \quad (17)$$

$$s = V_0 \cdot t \quad (18)$$

$$2 \quad t_1 \leq t \leq t_2$$

During this period the braking torque  $B = 0$  and the differential equation becomes:

$$\frac{d^2s}{dt^2} - n^2 \cdot s = \phi \quad (19)$$

The solution to equation (19) will commence from  $t = 0$  where  $t$  is given by

$$t = t_a - t_1 \quad (20)$$

For the particular integral we assume  $s = C$

$$s = C, \quad \frac{ds}{dt} = 0, \quad \frac{d^2s}{dt^2} = 0 \quad (21)$$

Substituting equations (21) in (19) we have

$$0 - n^2 \cdot C = \phi \quad (22)$$

$$\therefore C = -\frac{\phi}{n^2} \quad (23)$$

and the solution becomes

$$s = \alpha_1 \cdot \cosh(n \cdot t) + \beta_1 \cdot \sinh(n \cdot t) - \frac{\phi}{n^2} \quad (24)$$

$$v = \alpha_1 \cdot n \cdot \sinh(n \cdot t) + \beta_1 \cdot n \cdot \cosh(n \cdot t) \quad (25)$$

Now at  $t = 0$ , ( $t_a = t_1$ ) we have  $s = S_1$  and  $v = V_1$  where  $S_1$  and  $V_1$  can be found from equations (17) and (18) by lettering  $t = t_1$

Equations (24) and (25) now become:

$$S_1 = \alpha_1 \cdot 1 + \beta_1 \cdot 0 - \frac{\phi}{n^2} \quad (26)$$

$$V_1 = \alpha_1 \cdot n \cdot 0 + \beta_1 \cdot n \cdot 1 \quad (27)$$

giving

$$\alpha_1 = S_1 + \frac{\phi}{n^2} \quad (28)$$

$$\beta_1 = \frac{V_1}{n} \quad (29)$$

$$3 \quad t_2 \leq t_a \leq t_3$$

During this period the braking torque is a function of time  $t$ . The variation of braking torque against time is shown in Figure 3.

where  $t$  is given by

$$t = t_a - t_2 \quad (30)$$

The slope of the curve is given by

$$\text{Slope} = \frac{F}{t_3 - t_2} \quad (31)$$

$$\therefore B = \frac{F \cdot t}{(t_3 - t_2)} \quad (32)$$

and the differential equation becomes

$$\frac{d^2s}{dt^2} - n^2 \cdot s = \frac{\gamma \cdot F}{t_3 - t_2} \cdot t + \phi \quad (33)$$

and letting

$$\epsilon_1 = \frac{\gamma \cdot F}{t_3 - t_2} \quad (34)$$

we have

$$\frac{d^2s}{dt^2} - n^2 \cdot s = \epsilon_1 \cdot t + \phi \quad (35)$$

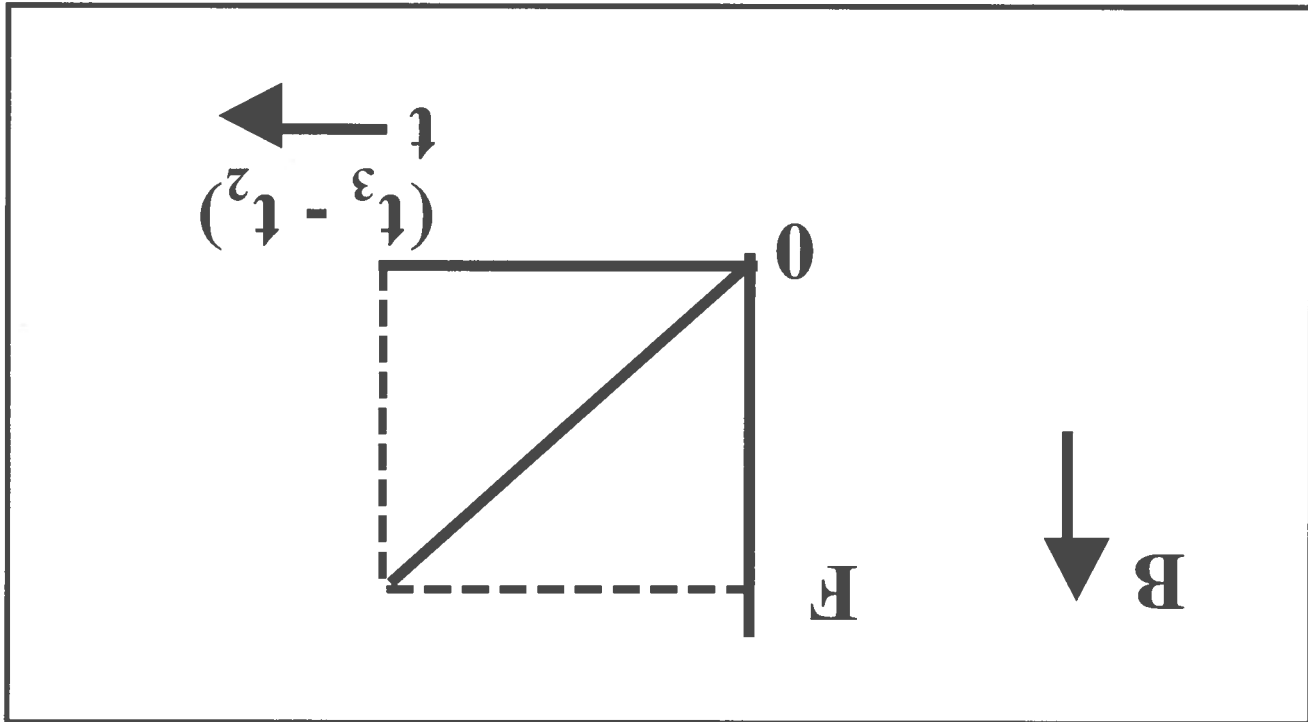


FIGURE 3  
Braking Torque vs Time

For the particular integral we assume  $s = C_1 t + D$

$$s = C_1 t + D, \quad \frac{ds}{dt} = C_1, \quad \frac{d^2s}{dt^2} = 0 \tag{36}$$

Substituting equations (36) into (35) we have:

$$v - n^2 (c \cdot t + D) = \epsilon_1 \cdot t + \phi \tag{37}$$

$$- n^2 \cdot c \cdot t + n^2 \cdot D = \epsilon_1 \cdot t + \phi \tag{38}$$

giving

$$C = - \frac{\epsilon_1}{n^2} \tag{39}$$

$$D = - \frac{\phi}{n^2} \tag{40}$$

The solutions are then:

$$s = \alpha_2 \cdot \cosh(n \cdot t) - \beta_2 \cdot \sinh(n \cdot t) - \frac{(\epsilon_1 \cdot t + \phi)}{n^2} \tag{41}$$

$$v = \alpha_2 \cdot n \cdot \sinh(n \cdot t) - \beta_2 \cdot n \cdot \cosh(n \cdot t) - \frac{\epsilon_1}{n} \tag{42}$$

Now at  $t = 0$ , ( $t_3 = t_2$ ) we have  $s = S_2$  and  $v = V_2$ , where  $S_2$  and  $V_2$  can be found from equations (24) and (25) by letting  $t = t_2 - t_1$ . Equations (41) and (42) then become:

$$S_2 = \alpha_2 \cdot 1 + \beta_2 \cdot 0 - \frac{\epsilon_1 \cdot 0 + \phi}{n^2} \tag{43}$$

$$V_2 = \alpha_2 \cdot n \cdot 0 - \beta_2 \cdot n \cdot 1 - \frac{\epsilon_1}{n} \tag{44}$$



giving

$$\alpha_2 = S_2 + \frac{\phi}{n^2} \quad (45)$$

$$\beta_2 = \frac{1}{n} \left( V_2 + \frac{\epsilon_1}{n^2} \right)$$

$$4 \quad t_3 \leq t_a$$

During this period the braking torque  $B = F$  the differential equation becomes

$$\frac{d^2s}{dt^2} - n^2 \cdot s = \gamma \cdot B + \phi \quad (47)$$

$$\text{and letting } \epsilon_2 = \gamma \cdot B + \phi \quad (48)$$

we have

$$\frac{d^2s}{dt^2} - n^2 \cdot s = \epsilon_2 \quad (49)$$

In the solution to equation (49)  $t$  is given by  $t = t_a - t_3$

For the particular integral we assume

$$s = C, \quad \frac{ds}{dt} = 0, \quad \frac{d^2s}{dt^2} = 0 \quad (50)$$

Substitution equation (50) into equations (49) we have:  $0 - n^2 \cdot C = \epsilon_2$  (51)

hence

$$C = - \frac{\epsilon_2}{n^2} \quad (52)$$

The solutions are then

$$s = \alpha_3 \cdot \cosh(n \cdot t) + \beta_3 \cdot \sinh(n \cdot t) - \frac{\epsilon_2}{n^2} \quad (53)$$

$$v = \alpha_3 \cdot n \cdot \sinh(n \cdot t) + \beta_3 \cdot n \cdot \cosh(n \cdot t) \quad (54)$$

Now at  $t = 0$  ( $t_a = t_3$ ) we have  $s = S_3$ , and  $v = V_3$  where  $S_3$  and  $V_3$  can be calculated from equations (41) and (42) by letting  $t = t_3 - t_2$

Equations (53) and (54) now become:

$$S_3 = \alpha_3 \cdot 1 + \beta_3 \cdot 0 - \frac{\epsilon_2}{n^2} \quad (55)$$

$$V_3 = \alpha_3 \cdot n \cdot 0 + \beta_3 \cdot n \cdot 1 \quad (56)$$

giving

$$a_3 = S_3 + \frac{\epsilon_2}{n^2} \quad (57)$$

$$\beta_3 = \frac{V_3}{n} \quad (58)$$

Using the above solutions the complete velocity/distance curve is defined.

## OBTAINING THE REQUIRED DATA AND APPROXIMATIONS

Most of the data required (for example mass of conveyance) should be readily available from the winder permit or reports from overwind tests or G.E.C. reports or the winder manual.

However, some items of data (for example inertia of the armature) may not be readily available and some difficulty may be experienced in obtaining it. It is the intention of this section to provide guidance on obtaining this data and failing this various approximations which can be used.

### Shaft Friction

The torque required for over-coming friction and windage depends on the condition of the shaft, conveyances, guides and sheaves as well as upon the winder speed. In practice this value of friction has been found to be from 5 % up to 25 or 30%.

As a rough guide for direct-coupled winders running at moderate speeds, the friction may be taken as being equal to an extra load of 5 to 7½ percent of the total suspended weight including pay load, conveyances and ropes; and for geared winders from 7½ to 10 percent.

The per unit value of friction used in the calculations will be given by

$$f =, \frac{\text{friction as a percentage}}{100} \quad 0 \leq F \leq 1$$

If the example shown in appendix 2, a friction value of  $f = 0.1$  was used.

### Coefficient of friction of brake linings

The coefficient of friction can be found by consulting tables for the appropriate material as supplied by the manufacturer.

In information from the manufacturer is not available the following approximations may be used.

Material	Oak	Poplar	Elm	Willow	Bonded Asbestos	Impregnated Fibre
coefficient	0,30	0,35	0,36	0,46	0,3	0,5

For the winder considered in the example in Appendix 2 the brake linings were Feroda Ltd., type CR linings with a coefficient of friction of 0,53.

### Inertias

If inertia figures are available from design data, manufacturers manuals or tests these should be used. However, if the information is not available the following approximations may be used.

#### a. Drums

The tables in appendix 1 give approximate values for the inertia and may be used with discretion.

#### b. Clutches, Drum Shafts:

For the clutches or drum shaft the moment of inertia can be calculated from:

$$I = \frac{m \cdot R^2}{4}$$

where  $m$  is the mass of the clutch or shaft  
 $R$  is the radius of the clutch or shaft

#### c. Gears:

If the mass and pitch diameter of the gear is known the inertia may be considered to be due to 60 percent of the total weight concentrated at the pitch circle.

$$I = 0.6 \times m \cdot k^2$$

$$m = \text{mass of gear}$$

$$k = \text{pitch circle radius}$$

d.

Armatures:

If the mass of the armature and the radius is known the inertia is given approximately by

$$I = m \cdot (0.75 \times r)^2$$

$$m = \text{mass of armature}$$

$$r = \text{radius of armature}$$

Having found the inertia of the armature it is necessary to refer this to the drum by multiplying by square of the gear ratio;

inertia of armature =  $m \cdot (0.75 \times r)^2 \cdot (\text{gear ratio})^2$  (referred to drums)

e.

Sheaves:

The tables given in Appendix 1 give approximate values of the inertia of sheaves.

f.

Load, Conveyance, Ropes:

The inertia of the load, conveyance and ropes vary throughout the wind and is a difficult quantity to calculate accurately. However, the following formulae may be used to give a reasonably close value.

Loads:  
Conveyances : mass of conveyance 1 + mass of conveyance 2

Loads : mass of load in  
conveyance 1 + mass of load in  
conveyance 2

rope : 2 x total length of one rope x mass per unit  
length

Total mass : sum of above mass = M

inertia I = 0.74 . M . R<sup>2</sup>

R = radius of drum

For the winder given in the example in Appendix 2 all the inertia values were obtained from manufacturers data except the inertia of the armatures and load, conveyances and ropes which were calculated using the above approximations. The calculations are shown in Appendix 2.

### Braking force

The braking force is the average force used to apply the brakes to the winder. Methods for estimating this will vary depending upon the type of brake configuration in use. As an example of how to calculate the braking force the reader should refer to the example in Appendix 2. This example is for a dead weight arrangement, although by using basic mechanical principles it should be possible to calculate the braking force for any system.

$t_1, t_2, t_3$

The dynamic braking deactuating time delay  $t_1$  can be found for the curves produced during an overwind test. For the example in Appendix 2 this was found to be one second. The time after the trip until brake shoe contact  $t_2$ , and the time to full braking force is applied  $t_3$  can be found by measuring the times at the winder.

### DISCUSSIONS AND CONCLUSIONS

The equations derived are sufficient to characterise the velocity/distance curve obtained during emergency braking without dynamic braking.

It should be remembered that as the velocity passes through zero the brake holding power will be sufficient to maintain the conveyance in a state of equilibrium and that any negative velocities predicted by the equations will not exist.

While the equations provide a mathematical analysis of the braking characteristics they are in themselves a first step only. Future development would include the incorporating of control functions into the mathematical model, as well as dynamic braking and other system functions.

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AN ENGINEERING DATA BOOK: by A J Munday and R A Farrar: The Macmillan Press Limited : 1979

**APPENDIX I**

**Moment of Inertia Values for Cylindrical Drums having Cast Cheeks and Steel Plate Barrels (from Broughton)**

For 1 drum only

Width M (ft)	1.83 (6)	2.13 (7)	2.44 (8)	2.74 (9)	3.05 (10)	3.35 (11)	3.66 (12)	3.96 (13)	4.27 (14)	4.57 (15)	4.88 (16)	
0.9 (3)	2.411	4.158	5.553	11.395	16.660	20.507	29.420	41.583				
1 (3.5)	2.519	4.309	5.824	12.055	17.879	22.254	30.612	43.208	60.411			
1.22 (4)	2.763	4.715	6.095	12.444	19.098	23.893	32.102	44.834	62.646	89.397		
1.37 (4.5)	2.871	4.863	6.772	12.834	20.317	25.465	33.456	46.757	64.880	91.767	126.239	
1.52 (5)	2.980	5.009	7.043	13.791	22.417	27.591	37.113	51.606	67.454	94.273	129.626	
1.83 (6)	3.332	5.563	7.585	14.569	23.636	29.162	39.822	54.993	76.665	106.870	146.015	
2.3 (7)	5.857	8.533	15.915	25.735	32.806	44.698		60.617	81.270	112.153	142.517	
2.44 (8)		9.075	16.815	27.090	34.675	47.272		64.203	90.413	125.156	168.906	
2.74 (9)			17.470	28.444	36.341	50.116		67.319	95.357	103.709	176.629	
3.05 (10)				29.799	38.197	51.877		70.773	99.962	138.159	184.483	
3.35 (11)					42.667	57.769		76.868	109.444	148.995	197.892	
3.66 (12)						49.439	64.610	88.855	126.646	175.543	231.619	
3.96 (13)							67.183	91.970	130.845	181.774	239.205	
4.27 (14)								69.486	135.450	180.419	245.842	
4.57 (15)									98.878	140.868	193.016	251.531
4.88 (16)									102.400	145.067	198.841	260.877

The above inertia values were obtained from Broughton. The values are in kg. m<sup>2</sup>. (GR<sup>2</sup>) i.e. the values in Broughton were converted from  $\frac{\text{lb} \times \text{ft}^2 \cdot \text{R}^2}{9}$  to kg. m<sup>2</sup>. (R<sup>2</sup>) by multiplying by

$$1.3545 \text{ i.e. } [\text{kg. m}^2 \cdot (\text{GR}^2) - 1.3545] \frac{\text{lb} \cdot \text{ft}^2}{9} (\text{GR}^2)$$

The above values for I are for the drum only (not shaft, clutch etc.)

**NOTE:**

The above values are low compared to those supplied by Vecor. This is due to the heavier construction used now.

For 1 drum (No Mechs)  $I_B \cdot \text{kg} \cdot \text{m}^2$ . (R<sup>2</sup>) =  $1.9 \times I_B \cdot \text{kg} \cdot \text{m}^2$ . (R<sup>2</sup>)

$$I_B = I \text{ from above table}$$

**Moment of Inertia  
Values supplied by Vecor**

Drum diameter M (ft)	Drum width M (ft)	Vecor I kg.m <sup>2</sup> .(R <sup>2</sup> ) 2 Drum + Mech	Vecor I kg.m <sup>2</sup> .(R <sup>2</sup> ) 2 Drums	Broughton 1 kg.m <sup>2</sup> .(R <sup>2</sup> ) 2 Drums
2.438 (8)	1.067 (3.5)	23 680	21 312	11 648
2.75 (9)	1.22 (4)	44 760	40 284	24 888
3.96 (13)	1.98 (6.5)	244 130	219 717	116 758
4.27 (14)	1.22 (4)	268 600	241 740	125 292
4.92 (16)	1.32 (4.5)	490 500	441 450	252 478
4.92 (16)	1.64 (5.5)	515 000	463 500	278 214
5.5 (18)	1.83 (6)	881 600	793 440	NOT SUPPLIED IN TABLE
5.5 (18)	2 (6.5)	922 270	830 043	NOT SUPPLIED IN TABLE

**NOTE:**

The values supplied by Vecor are for 2 Drums + Mechs. Vecor informed the writer the mechanical parts, shaft, clutch etc., accounted for approximately 10% of the value.

COLUMN 1 Indicates kg. m<sup>2</sup> for 2 Drums + Mech  
COLUMN 2 Indicates kg . m<sup>2</sup> for 2 drums

**Diameters and Inertia Values for Sheave Wheels  
Supplied by B. Thomas and Pilliner Engineering**

**STANDARD DUTY**

Sheave diameter (mm) (ft)	Moment of kg . m <sup>2</sup> . (GR <sup>2</sup> )
1 830 (6')	566
2 438 (8')	1 518
2 743 (9')	3 030
3 048 (10')	4 080
3 658 (12')	6 550
3 962 (13')	11 890
4 267 (14')	15 850
4 877 (16')	24 100
5 500 (18')	32 300

**HEAVY DUTY**

Sheave diameter (mm) (ft)	Moment of inertia kg . m <sup>2</sup> . (R <sup>2</sup> )
3 048 (10')	4 397
3 658 (12')	7 130
4 267 (14')	17 100
4 877 (16')	25 700
5 500 (18')	35 000
5 790 (19')	40 000
6 100 (20')	44 000

APPENDIX 2

**Example: Buffelsfontein Gold Mine Pioneer Shaft 5 + 6 Winder Left Hand Lilly Lower Limits.**

It was decided to test the derived formulae by calculating speed/distance curves and comparing these with the curves measured by Gencor Group Winder Department on 5 November 1985.

Most of the information required was readily available from the winder permit, test results and manufacturers data.

Other information was calculated as follows:

**Distance from end of wind at trip**

At the time of the trip the position of the conveyance is illustrated in Figure 4.

By adding the three distances illustrated in Fig 4 the total distance from the end of wind can be found.

**Inertias**

All the inertia values were obtained from manufacturers data except the following which were calculated as shown.

**Armatures**

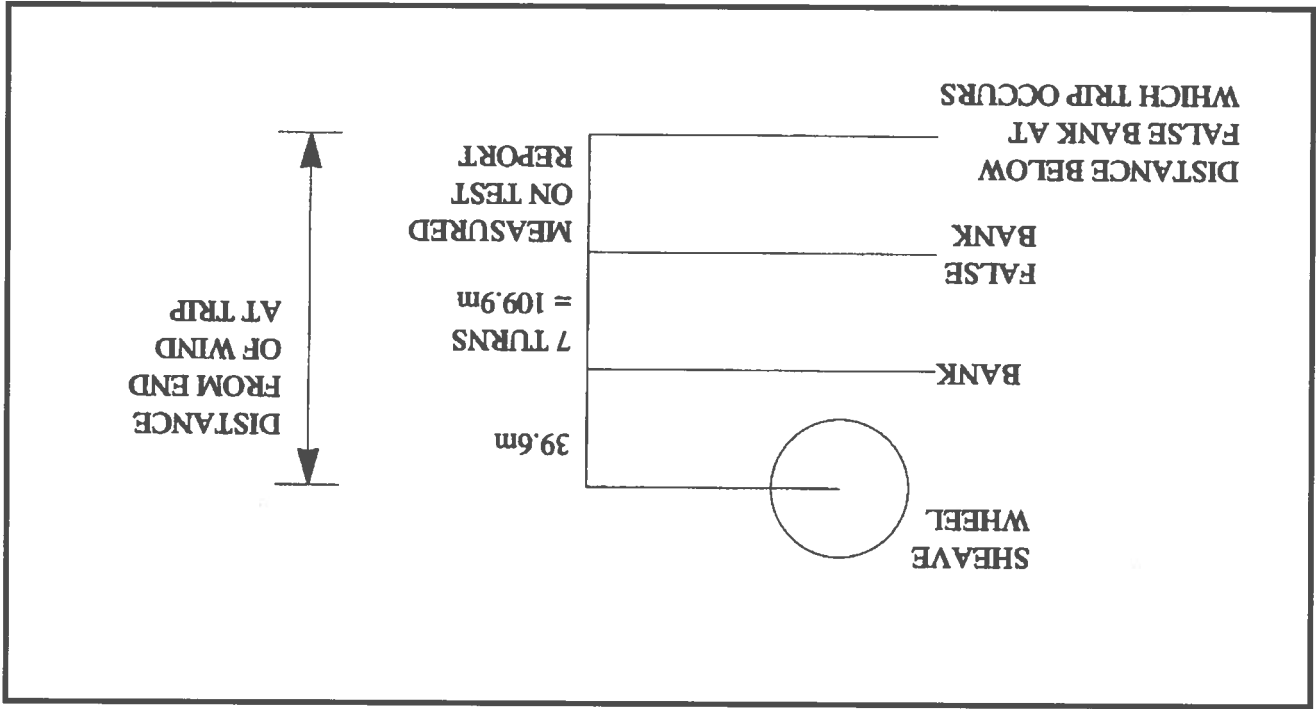
From engineering drawings it was found that the mass of the armature = 8 845 kg and the radius = 0.45m and from the maintenance manual the gear ratio was found to be 8.204:1.

We therefore have:

$$\begin{aligned} \text{Inertia of one armature} &= \text{mass} \times (0.75 \times \text{radius})^2 \\ &= 8\ 845 \times (0.75 \times 0.45)^2 \\ &= 1\ 023 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

$$\begin{aligned} \text{Inertia of two armatures} &= 2 \times 1\ 023 \\ &= 2\ 046 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

FIGURE 4  
Position of conveyance at time of trip



$$\begin{aligned} \text{Total inertia referred to drum} &= \text{inertia of armature} \times (\text{gear ratio})^2 \\ &= 2\,046 \times (8.204)^2 \\ &= 137\,707 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

### Gears

From the manufacturers data the inertia of the gear wheel is 31 153 kg · m<sup>2</sup> · (GR<sup>2</sup>) and the inertia of each pinion is 54 kg · m<sup>2</sup> · (GR<sup>2</sup>). The gear ratio is 8.204:1.

$$\begin{aligned} \text{Inertia of two pinions} &= 2 \times 54 \\ &= 108 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \\ \text{Inertia of pinions referred to drum} &= \text{inertia} \times (\text{gear ratio})^2 \\ &= 108 \times 8\,204^2 \\ &= 7\,269 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

$$\begin{aligned} \text{Total inertia of gears} &= \text{inertia of gear wheel} + \text{inertia of pinions} \\ &\text{referred to drum} \\ &= 31\,153 + 7\,269 \\ &= 38\,422 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

### Sheaves

From the maintenance manual the inertia of each sheave is 7 450 kg · m<sup>2</sup> · (GR<sup>2</sup>) and the sheave diameter is 5.48m and the diameter of the drum is 4.88m. Therefore we have :

$$\begin{aligned} \text{Inertia of 2 sheaves} &= 2 \times 7\,450 \\ &= 14\,900 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

$$\begin{aligned} \text{Total inertia referred to drums} &= \text{inertia of sheaves} \left( \frac{\text{sheave diameter}}{\text{drum diameter}} \right)^2 \\ &= 14\,900 \times \left( \frac{5.48}{4.88} \right)^2 \\ &= 18\,789 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

### Load Conveyances, Ropes:

The approximate inertia of the load, conveyances and drums is as follows:

From the winder permit the mass of the skip and attachments is 7 565 kg and the net load during the tests was 3 855 kg. The total length of the rope is 1 950 m and the mass per unit length is 10.4 kg/m

This gives:

$$\begin{aligned} \text{Mass of two conveyances} &= 2 \times 7\,565 &= 15\,130 \\ \text{Net load} &= 3\,855 &= 3\,855 \\ \text{Mass of two ropes} &= 2 \times 1\,950 \times 10.4 &= 40\,560 \\ \text{TOTAL MASS} &= 59\,545 \text{ kg} \end{aligned}$$

The mean radius of the drum is 2.5m and this gives an inertia of:

$$\begin{aligned} \text{inertia} &= 0.74 \times \text{Total mass} \times (\text{mean radius})^2 \\ &= 0.74 \times 59\,545 \times 2.5^2 \\ &= 275\,396 \text{ kg} \cdot \text{m}^2 \cdot (\text{GR}^2) \end{aligned}$$

### Braking Force:

The braking arrangement for the winder is shown in Figure 5. From this we can obtain the following information.

$$\begin{aligned} \text{The volume of the mass} &= 0.9 \times 0.49 \times 0.68 \\ &= 0.3 \text{ m}^3 \end{aligned}$$

Taking the density of mild steel as 7 850 kg/m<sup>3</sup> this gives:

$$\begin{aligned} \text{mass of weight} &= \text{density} \times \text{volume} \\ &= 7\,850 \times 0.3 \\ &= 2\,355 \text{ kg} \end{aligned}$$

$$\begin{aligned} \text{The force due to this mass} &= g \times \text{mass} \\ &= 9.81 \times 2\,358 \\ &= 23\,103 \text{ N} \\ &= 23.1 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{The mechanical advantage of the lever arm} &= \frac{2.38}{0.28} \\ &= 8.5 \end{aligned}$$

$$\begin{aligned} \text{The mechanical advantage of the bellcrank} &= \frac{1.63}{0.41} \\ &= 3.98 \end{aligned}$$

$$\begin{aligned} \text{force} &= 23.1 \times 8.5 \times 3.98 \\ &= 782 \text{ kN} \end{aligned}$$

This is the braking force for one set of brakes, therefore the total braking force is equal to twice this.

$$\begin{aligned} \text{Total braking force} &= 2 \times 782 \\ &= 1\,564 \text{ kN} \end{aligned}$$

### Braking Times

The deactuating time delay was measured from the overwind test and found to be 1s.

In order to establish the time until brake shoe contact and the time until full braking force is applied the braking times turn for turn were measured at the winder and the curves obtained are shown in Figure 6. The brake times were measured from the average of the two curves for the right hand and left hand brakes.

Because the cam position is relative to the false bank the distance of the tip from the false bank was converted into turns and this was used to find the brake times.

### Input Data:

The following is a summary of all the necessary information required to calculate the speed/distance curves.

$$\begin{aligned} \text{Mass of conveyance 1} &= 7\,565 \text{ kg} \\ \text{Mass of conveyance 2} &= 7\,565 \text{ kg} \end{aligned}$$

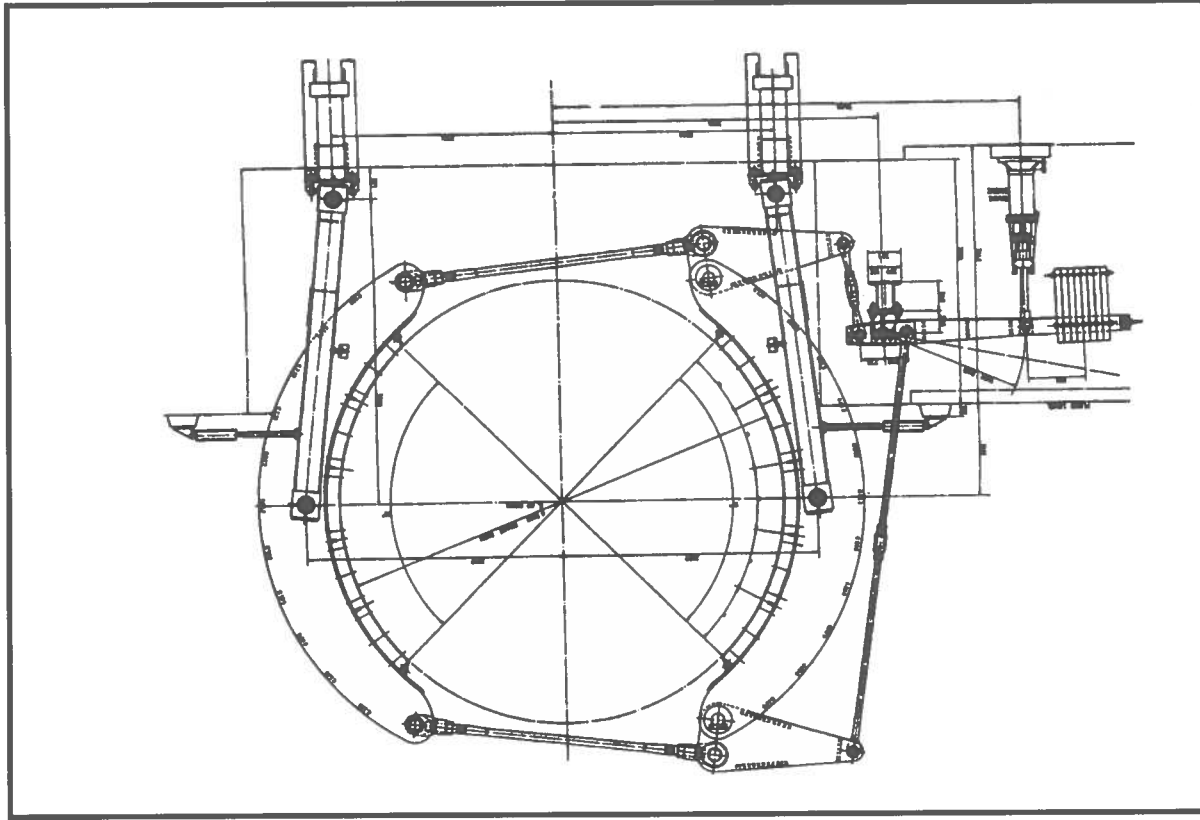


FIGURE 5  
Arrangement of Brake Gear



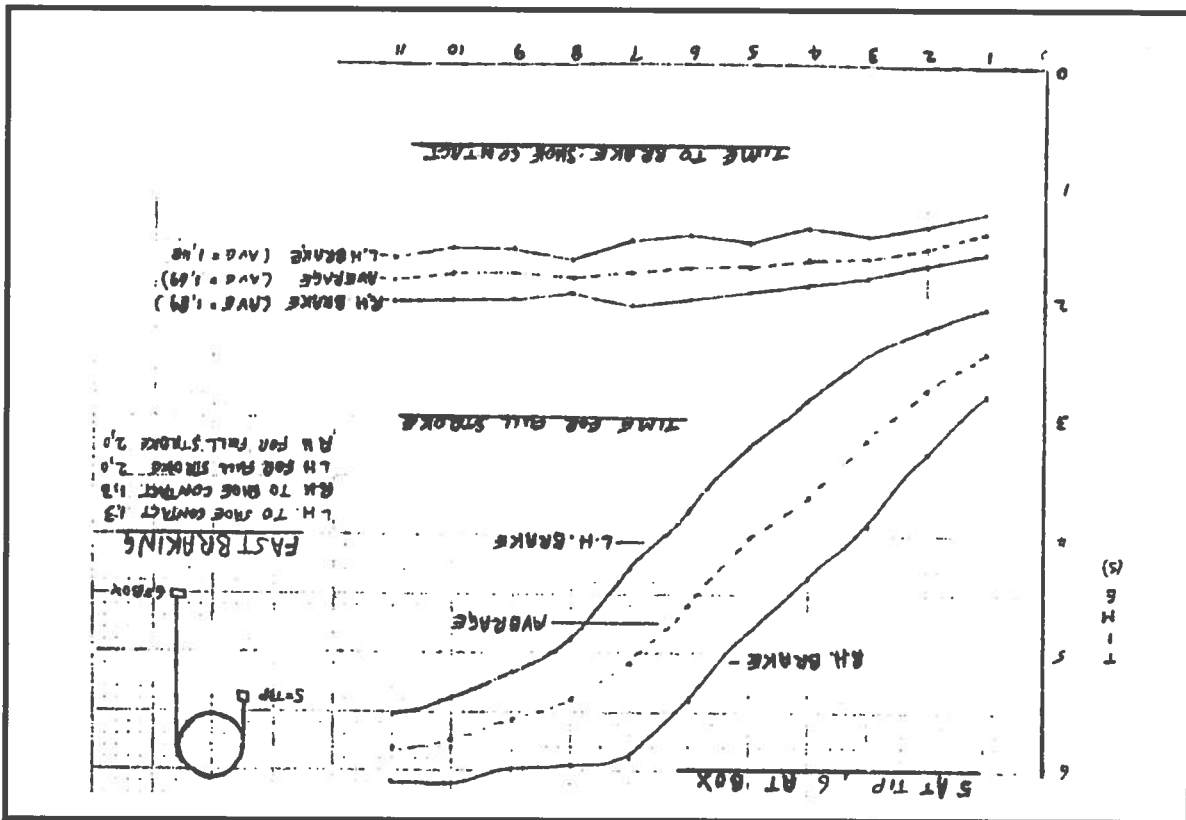


FIGURE 6  
Brake times 5 and 6 Winder

- Load in conveyance 1 = 3 855 kg
- Load in conveyance 2 = 0 kg
- Length of wind = 1 588.3 m
- Mass per unit length of rope = 10.4 kg/m
- Friction allowance = 0.1
- Radius of drum = 2.44 m
- Radius of brake path = 2.6 m
- Coefficient of friction of brake linings = 0.53
- Inertia of drums = 474 075 kg · m<sup>2</sup> · (GR<sup>2</sup>)  
(including clutches + shaft)
- Inertia of armatures = 137 707 kg · m<sup>2</sup> · (GR<sup>2</sup>)
- Inertia of gears = 38 422 kg · m<sup>2</sup> · (GR<sup>2</sup>)
- Inertia of sheaves = 18 789 kg · m<sup>2</sup> · (GR<sup>2</sup>)
- Inertia of load, ropes and conveyances = 275 396 kg · m<sup>2</sup> · (GR<sup>2</sup>)
- Braking force = 1 564 kN
- Dynamic braking deactuating time delay = 1 s

Trip velocity (m/s)	Distance of trip from end of wind (m)	Time after trip until brake shoe contact (s)	Time after trip until full braking (s)
15.0	269.5	1.63	5.3
8.2	200.5	1.63	3.35
3.8	167.5	1.43	2.3

Computer Program

Due to the large number of calculations involved a computer program was written. The machine used is a Hewlett Packard 85 and a listing of the program is shown in Appendix 3.

Results:

Using the computer program the curves for the 3 different trip speed were calculated and plotted against the experimental curves. The results are shown in Appendix 4.

All three sets of curves appearing in Appendix 4 are superimposed onto one graph in Figure 7.

**Discussion:**

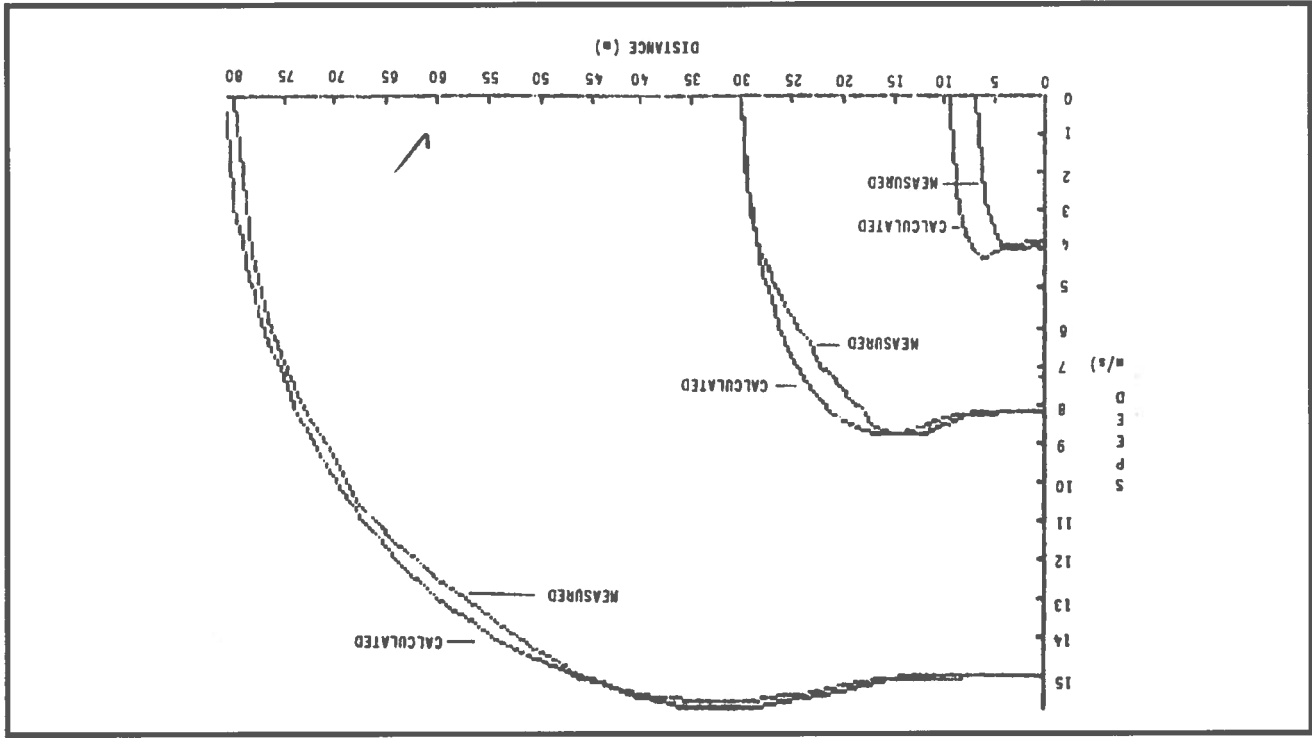
As can be seen from Figure 7 the calculated curves and the experimental curves do in fact coincide.

This shows that the equations derived are correct and that applying the laws of physics to the problem of winder braking does give the correct answer.

**Conclusion**

The techniques outlined in this report are adequate for simulating emergency braking characteristics without the use of dynamic braking.

FIGURE 7



COMPUTER PROGRAM

Program Listing

```

5 CLEAR
6 DISP "EMERGENCY BRAKING
CALCULATIONS"
7 DISP "-----"
8 DISP @ DISP "BY S.M. MCFADYEN
"@ INPUT C1
10 DISP "INPUT MASS OF
CONVEYANCE 1" @ INPUT C1
20 DISP "INPUT MASS OF
CONVEYANCE 2 "
@ INPUT C2
30 DISP "INPUT MASS OF LOAD IN
CONVEY 1 " @ INPUT M1
40 DISP "INPUT LENGTH OF WIND"
CONVEY2" @ INPUT M2
50 DISP "INPUT LENGTH OF WIND"
@ INPUT L
60 DISP " INPUT MASS PER METRE OF
ROPE " @ INPUT M
70 DISP "INPUT DIST OF TRIP FOR
M EOW" @ INPUT X0
80 DISP "INPUT FRICTION ALLOWANCE
(0-1)" @ INPUT D1
90 DISP " INPUT RADIUS OF DRUM"
@ INPUT R
100 DISP " INPUT RADIUS OF BRAKE
PATH" @ INPUT R1
110 DISP "INPUT COEFF OF FRICT. FOR
BRAKES" @ INPUT U
120 DISP "INPUT INERTIA OF DRUMS"
@ INPUT I1
130 DISP " INPUT INERTIA OF CLUTCHES"
@ INPUT I2
140 DISP "INPUT INERTIA OF DRUM
SHAFT" @ INPUT I3

```

```

150 DISWP " INPUT INERTIA OF ARMATURES"
@ INPUT I4
160 DISP "INPUT INERTIA OF GEARS"
@ INPUT I5
170 DISP "INPUT INERTIA OF SHEAVES"
@ INPUT I6
180 DISP "INPUT INERTIA OF LOAD,
ROPE, ETC" @ INPUT I7
190 DISP " INPUT BRAKING FORCE
APPLIED" @ INPUT F1
2000 REM
2010 REM PLOT OUT CURVES
2020 REM
2100 REM
2110 REM FILL RRY X2,Y2
2120 TO = 0 @ N1 = 0
2125 IF T0 <= T1 THEN T = T0
2130 IF T0 <= T1 THEN GOSUB 3000
2140 IF T0 <= T1 THEN 2000
2145 IF T0 <= T2 THEN T = T0 - T1
2150 IF T0 <= T2 THEN GOSUB 4000
2160 IF T0 <= T2 THEN 2200
2164 IF T0 < T3 THEN T = T0 - T2
2165 IF T0 < T3 THEN GOSUB 5000
2166 IF T0 < T3 THEN 2200
2169 T = T0 - T3
2170 GOSSUB 5500
2200 IF V < 0 THEN 3200
2210 N1 = N1 + 1 @ X2(N1) = S @
Y2(N1) = V
2220 T0 = T0 + 1
2230 GOTO 213 0
2300 REM
2310 REM FIND MAXIMUM AND
2320 REM MAXIMUM VALUES OF S
2330 REM AND V
2340 EM
2350 Z1 = 0 @ Z2 = 0 Z3 = 0 @
Z4 = 0
2360 FOR J = 1 TO N0
2370 IF X 1 (J) > Z3 THEN Z3 = X1 (J)
2380 IF Y1 (J) > Z4 THEN Z4 = Y1 (J)

```

```

2390 NEXT J
2400 FOR J = 1 TO N1
2410 IF X 2(J) > Z3 THEN Z3 = X2 (J)
2420 IF Y2(J) > Z4 THEN Z4 = Y2 (J)
2430 NEXT J
2500 REM
2510 REM PLOT CURVES
2520 REM
2525 GCLEAR
2530 SCALE Z1, Z3, Z2, Z4
2540 XAXIS 0.5 @ YAXIS 0,1
2600 REM
2610 REM PLOT EXPERIMENTAL
2620 REM DATA
2630 REM
2640 MOVE X1(I), Y1(I)
2650 FOR J = 1 TO N0
2660 DRAW X 1 (J), Y 1 (J)
5030 REM
5040 Q3 = Q1*F1/(T3-T2)
5070 A2 = S2 + Q2/(N*N)
5080 B2 = (V2+Q3/(N*N))/N
5090 H1 = (EXP(N*T) + EXP(-N*T))/2
5100 H2 = (EXP(N*T) - EXP(-N*T))/2
5110 S = A2*H1+B1*H2 - (Q3*T+Q2)/
5120 V = A2*N*H2+B2 NH1Q3/(N*N)
5130 RETURN
5500 REM
5510 REM SUBROUTINE FOR S AN DV
5520 REM FOR T3<T-&&&&
5530 REM
5540 Q5 = A1*F1+Q2
5570 A3 = S3 + Q5/(N*N)
5580 B3 = V3/N
5585 H1 = (EXP(N*T)+EXP(-N*T))/2
5586 H2 = (EXP(N*T)-EXP(-N*T))/2
5590 S=A3*H1+B3*H2 - Q5/(N*N)
5600 V = A3*N*H2+b3*N*H1
5610 RETURN
6000 REM
6010 REM PRINT OUT DATA
6020 REM
2875 PRINT @ PRINT
2876 PRINT : "-----"
2877 PRINT "-----"
2900 REM
2910 REM END OF PROGRAM
2920 REM FOR 0<T<T1
2930 GOTO 9 999
3000 REM
3010 REM SUBROUTINE FOR S
AND V
3020 REM FOR 0 <T<T1
3030 REM
3040 V = V0
3050 S = S = V0 T
3080 RETURN
4000 REM
4010 REM SUBROUTINE FOR S
AND V
4020 REM FOR T1 <T<T2
4030 REM
4060 A1 = S1 + Q2/(N N)
4070 B1 = V1/N
4080 H1 = (EXP(N T) + EXP (-N
T)/2
4090 h2 = exp(n t) - EXP(-N T)/
2
4100 S = A1 H1 + B1 H1 - Q2/
(N N)
4110 V = A1 N H2 + B1 N H1
4120 RETURN
5000 REM
5010 REM SUBROUTINE FOR S
AND V
5020 REM FOR T2, T, T3
6290 PRINT "TIME DELAY=";
T1
6300 PRINT "TIME AFTER
TRIP UNTIL BRAKE"
6310 PRINT "SHOE
CONTACT="; T2
6320 PRINT "TIME TO FULL
BRAKING TORQUE"
6030 PRINT @ PRINT 6330 PRINT "IS APPLIED=";
6040 PRINT "-----" T3
6050 PRINT "-----" 6340 PRINT "INITIAL
VELOCITY="; V0
6060 PRINT @ PRINT @ PRINT PRINT @ PRINT @ PRINT
6070 PRINT "MASS OF CONVEYANCE 1="; C1 6350 (N*N) RETURN
6080 PRINT "MASS OF CONVEYANCE 2 ="; C2
6090 PRINT "LOAD OF CONVEYANCE 1 ="; M1 6400
6100 PRINT "LOAD OF CONVEYANCE 2="; L 9999 END
6110 PRINT "LENGTH OF WIND="; M2
6120 PRINT "MASS PER UNIT LENGTH OF ROPE="; M
6130 PRINT "DISTANCE OF TRIP FROM END OF"
6140 PRINT "WIND="; X0
6150 PRINT "FRICTION ALLOWANCE="; D1
6160 PRINT "RADIUS OF DRUM="; R
6170 PRINT "RADIUS OF BRAKE PAT="; R1
6180 PRINT "COEFFICIENT OF FRICTION="; U
6190 PRINT "INERTIA OF DRUMS="; I1
6200 PRINT "INERTIA OF CLUTCHES="; I2
6210 PRINT "INERTIA OF DRUM SHAFT="; I3
6220 PRINT "INERTIA OF ARMATURES="; I4
6230 PRINT "INERTIA OF GEARS="; I5
6240 PRINT "INERTIA OF SHAVES="; I6
6250 PRINT "INERTIA OF LOAD, ROPES AND"
6260 PRNT "CONVEYANCES="; I7
6270 PRINT "BRAKING FORCE="; F1
6280 PRINT "DYNAMIC BRAKING DEACTUATING"

```

### Program Variables

As an aid to understanding the program the following is a list showing each program variables in alphabetical order and the actual variable it represents;

Program variable	Variable it represents	Program variable	Variable it represents
A1	$\alpha_1$	Q1	$\gamma$
A2	$\alpha_2$	Q2	$\psi$
A3	$\alpha_3$	Q3	$\epsilon_1$
B1	$\beta_1$	Q5	$\epsilon_2$
B2	$\beta_2$	R	R
B3	$\beta_3$	R1	$R_b$
C1	$C_1$	S	s
C2	$C_2$	S1	$S_1$
D1	f	S2	$S_2$
F1	F	S3	$S_3$
F\$	name of file containing experimental data	T	t
G	gravitational constant = 9.80665	T0	$t_a$
H1	cosh (n,t)	T1	$t_1$
H2	sinh (n,t)	T2	$t_2$
I	program loop counter	T3	$t_3$
I0	$I_t$	U	$\mu$
I1	$I_d$	V	v
I2	$I_c$	V0	$V_0$
I3	$I_s$	V1	$V_1$
I4	$I_a$	V2	$V_2$
I5	$I_g$	V3	$V_3$
I6	$I_{sh}$	X0	$X_0$
I7	$I_r$	X1	array containing experimental distance values
J	program loop counter	X2	array containing calculated distance values
L	l	Y1	array containing experimental velocity values
M	m	Y2	array containing calculated velocity values
M1	$M_1$	Z1	variable containing minimum distance value
M2	$M_2$	Z2	variable containing minimum velocity value
N	$n (= \sqrt{nr})$	Z3	variable containing maximum distance value
N0	number of data points in experimental data	Z4	variable containing maximum velocity value
N1	a program counter		

### Data File

The experimental points need to be first placed in a data file so that the program can read them in. The format of the data file is as follows:

```

1st rec      :      < number of data points (n)
2nd rec      :      < dist (1) > , < vel (1) >
3rd rec      :      < dist (2) > , < vel (2) >
4th rec      :      < dist (3) > , < vel (3) >
5th rec      :      < dist (4) > , < vel (4) >
6th rec      :      < dist (5) > , < vel (5) >
7th rec      :      < dist (6) > , < vel (6) >
8th rec      :      < dist (7) > , < vel (7) >
nth rec      :      < dist (n - 1) > , < vel (n - 1) >
(n + 1) rec  :      < dist (n) > , < vel (n) >
    
```

A simple program for creating the data file is shown below:

```

10  REM
20  REM WRITE A DATA FILE FOR
30  REM EXPERIMENTAL DATA FOR
40  REM USE
IN PROGRAM BRAKES
50  REM
70  CLEAR
80  DISP
85  DISP "Note file must not exist"
90  DISP "FILE NAME TO SAVE DATA IN":
@ INPUT F$
100 DISP
110 DISP "IN RESPONSE TO PROMPT
"??" INPUT
120 DISP "THE NEXT DISTANCE AND
VELOCITY"
130 DISP "VALUES. THE VALUES MUST
BE INPUT"
140 DISP "IN CORRECT SEQUENCE
AND NO"
150 DISP "EDITTING FACILITIES EXIST"
160 DISP "TO END ENTERING DATA
INPUT 0.0"
170 DISP
260 GOTO 195
300 CLEAR
310 DISP "MAXIMUM
NUMBER OF DATA
POINTS
DISP @ DISP
"PROGRAM WILL
AUTOMATICALLY SAVE"
DISP "DATA"
FOR I = 1 TO 1000 @
NEXT I
350 GOTO 500
500 REM
510 REM SAVE DATA
520 REM
530 CLEAR
540 DISO "SAVING DATA"
542 N0 = N0 - 1
541 FOR I = 1 TO 500 @
NEXT I
545 R=N0+1
546 CREATE FS.R.16
550 ASSIGN # 1 TO F$
555 PRINT # 1, N0
    
```

```

180 DIM X (100), Y (100)
190 N0 = 1
195 IF NO>100 THEN 300
200 DISP "?": @ INPUT X (N0), Y (N0)
210 IF X (N0)=0 THEN 240
220 N0=N0+1
230 GOTO 195
240 IF Y (N0)=0 THEN 500
250 N0=N0+1
560 FOR I = 1 TO N0
570 PRINT #1, X (I), Y (I)
580 NEXT I
590 ASSIGN #1 TO I0*
600 CLEAR
610 DISP "END OF PROGRAM"
620 DISP @ DISP "BYE BYE"
630 END

```

RESULTS:

15m/s TRIP

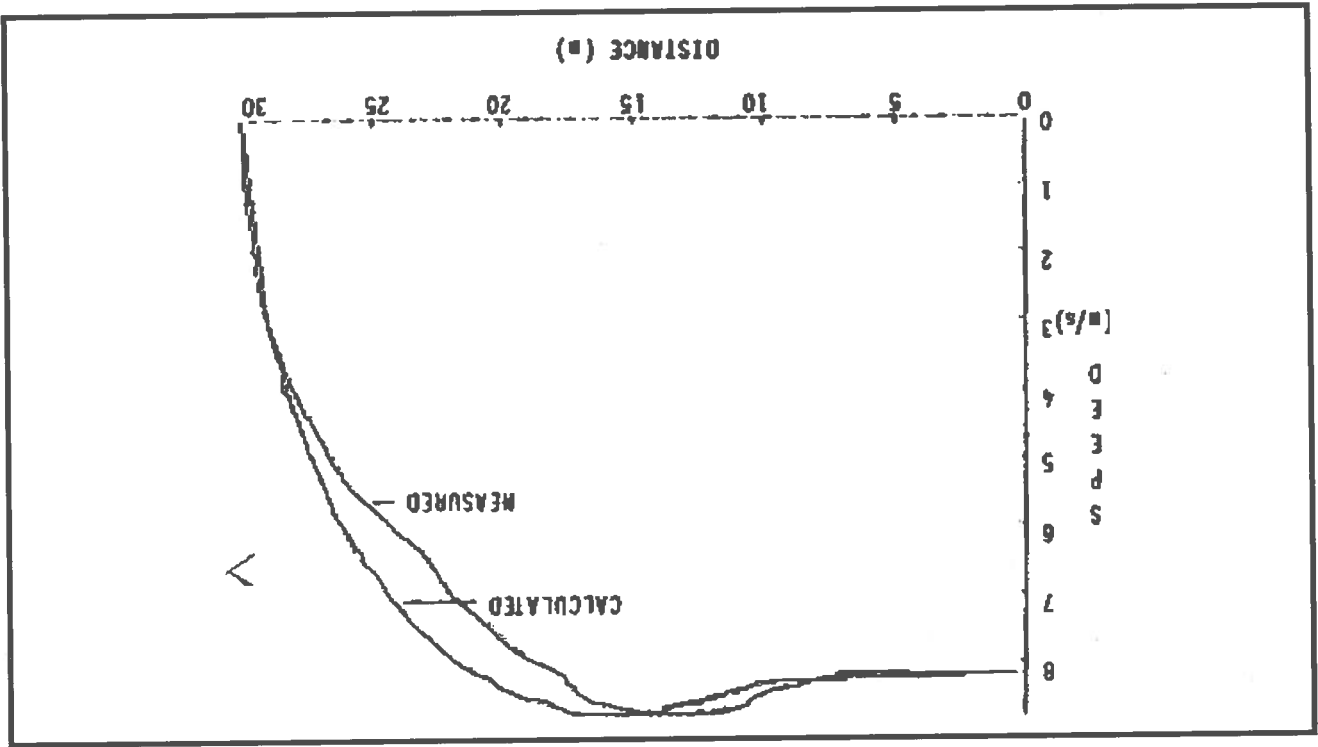
MASS OF CONVEYANCE 1 = 7565  
 MASS OF CONVEYANCE 2 = 7565  
 LOAD IN CONVEYANCE 1 = 3955  
 LOAD IN CONVEYANCE 2 = 0  
 LENGTH OF WIND = 1588.3  
 MASS PER UNIT LENGTH OF ROPE = 10.4  
 DISTANCE OF TRIP FROM END OF WIND = 269.5  
 FRICTION ALLOWANCE = .1  
 RADIUS OF DRUM = 2.44  
 RADIUS OF BRAKE PATH = W.6  
 COEFFICIENT OF FRICTION = .53  
 INERTIA OF DRUMS = 474075  
 INERTIA OF CLUTCHES = 0  
 INERTIA OF DRUM SHAFT = 0  
 INERTIA OF ARMATURES = 137707  
 INERTIA OF GEARS = 38422  
 INERTIA OF SHEAVES = 18789  
 INERTIA OF LOAD, ROPES AND CONVEYANCES = 27396  
 BRAKING FORCE = 1564000  
 DYNAMIC BRAKING DEACTUATING  
 TIME DELAY =  
 TIME AFTER TRIP UNTIL BRAKE  
 SHOE CONTACT = 1.63  
 TIME TO FULL BRAKING TORQUE  
 IS APPLIED = 5.3  
 INITIAL VELOCITY = 15

8.2 m/s TRIP

MASS OF CONVEYANCE 1 = 7565  
 MASS OF CONVEYANCE 2 = 7565  
 LOAD IN CONVEYANCE 1 = 3955  
 LOAD IN CONVEYANCE 2 = 0  
 LENGTH OF WIND = 1588.3  
 MASS PER UNIT LENGTH OF ROPE = 10.4  
 DISTANCE OF TRIP FROM END OF WIND = 200.5  
 FRICTION ALLOWANCE = .1  
 RADIUS OF DRUM = 2.44  
 RADIUS OF BRAKE PTH = 2.6  
 COEFFICIENT OF FRICTIN = .53  
 INERTIA OF DRUMS = 474075  
 INERTIA OF CLUTCHES = 0  
 INERTIA OF DRUM SHAFT = 0  
 INERTIA OF ARMATURES = 137707  
 INERTIA OF GEARS = 38422  
 INERTIA OF SHEAVES = 18789  
 INERTIA OF LOAD, ROPES AND CONVEYANCES = 275396  
 BRAKING FORCE = 1564 000  
 DYNAMIC BRAKING DEACTUATING  
 TIME DELAY = 1  
 TIME AFTER TRIP UNTIL BRAKE  
 SHOE CONTACT = 1.63  
 TIME TO FULL BRAKING TORQUE  
 IS APPLIED = 3.35  
 INITIAL VELOCITY = 8.2

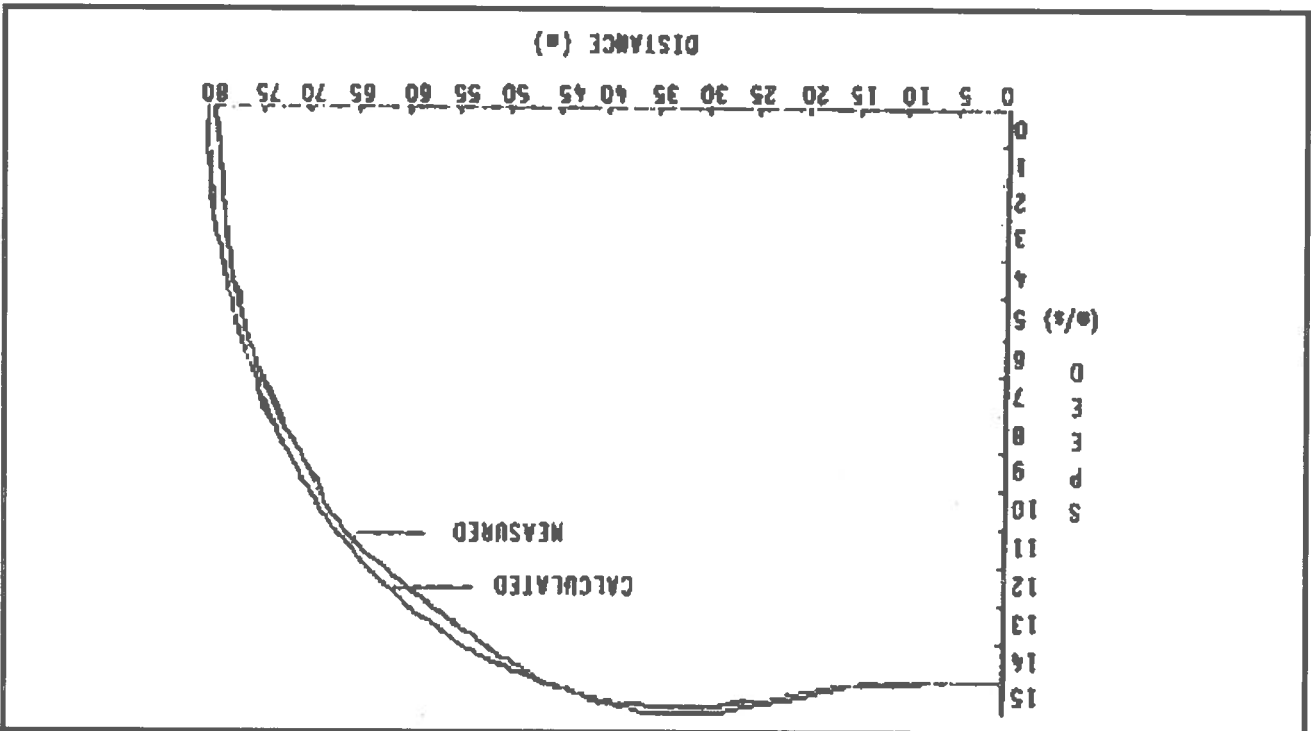
8.2 m/s Trip

FIGURE 9



15 m/s Trip

FIGURE 8



### 3.8 M/S TRIP

MASS OF CONVEYANCE 1 = 7565  
MASS OF CONVEYANCE 2 = 7565  
LOAD IN CONVEYANCE 1 = 3855  
LOAD IN CONVEYANCE 2 = 0  
LENGTH OF WIND = 1 588.3  
MASS PER UNIT LENGTH OF ROPE = 10.4  
DISTANCE OF TRIP FROM END OF WIND = 167.5  
FRICTION ALLOWANCE = .1  
RADIUS OF DRUM = 2.44  
RADIUS OF BRAKE PATH = 2.6  
COEFFICIENT OF FRICTION = .53  
INERTIA OF DRUMS = 474075  
INERTIA OF CLUTCHES = 0  
INERTIA OF DRUM SHAFT = 0  
INERTIA OF ARMATURES = 137707  
INERTIA OF GEARS = 38422  
INERTIA OF SHEAVES = 18789  
INERTIA OF LOAD, ROPES AND  
CONVEYANCES = 275396  
BRAKING FORCE = 1564000  
DYNAMIC BRAKING DEACTUATING  
TIME DELAY = 1  
TIME AFTER TRIP UNTIL BRAKE  
SHOE CONTACT = 1.43  
TIME TO FULL BRAKING TORQUE  
IS APPLIED = 2.3  
INITIAL VELOCITY = 3.8

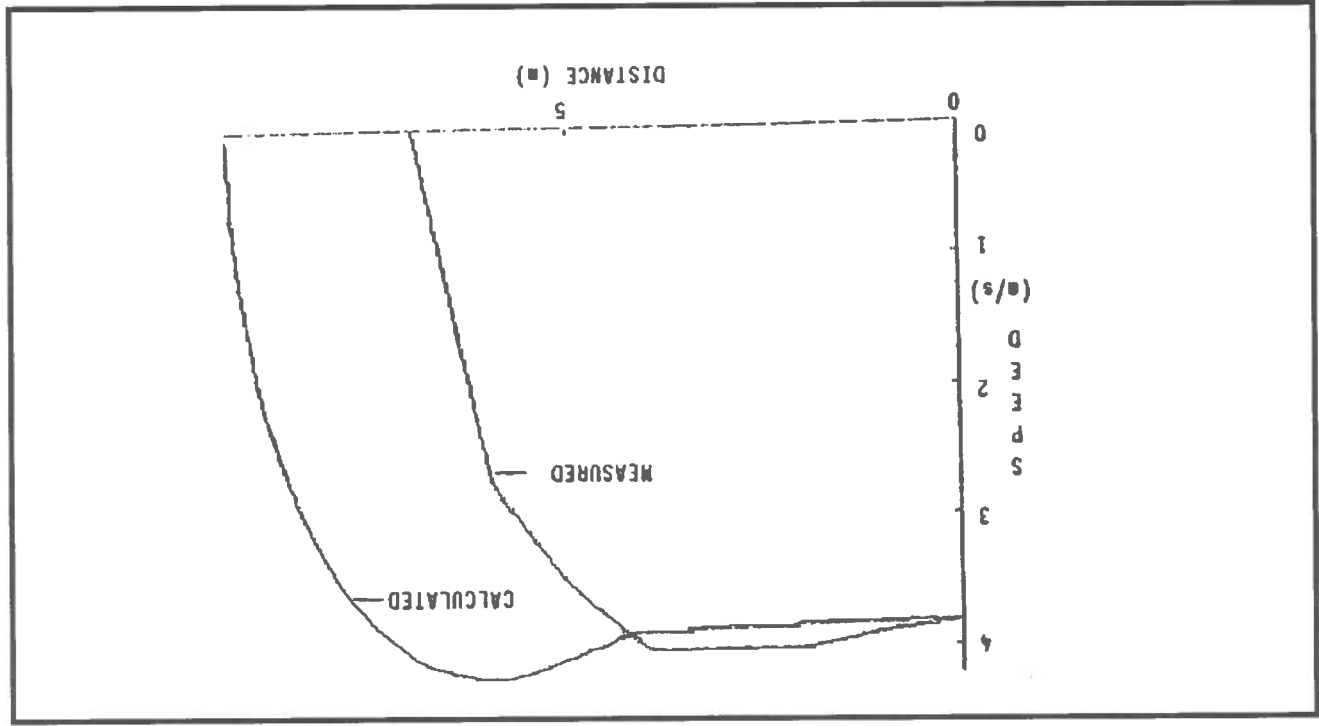


FIGURE 10  
3.8 m/sec Trip



APPENDIX 5

RUN IN TESTS TO PROVE END-OF WIND PROTECTION

Observations	Recommendations/Action
<p>1. Although the safety margin of not less than 40% was satisfied by all tests high average rates of deceleration were recorded.</p> <p>This condition is caused by the long brake delay after tripout.</p>	<p>1. It is recommended, (as was done in the previous report of 9.11.84) that a cage mounted decelerometer brake test should be carried out to obtain optimum brake settings for this winder.</p>

Inspector's Remarks

Arrangements need to be made with the Head Office Winder Department to set a data for carrying out the decelerometer brake test.

BRAKE AND CONTROLLER SETTINGS AT COMMENCEMENT OF TEST

False landing position: Drum diameter 4.88 m  
 Full speed 16.2 m/s 3 200 ft/min  
 Turns above or below end of wind 7.0 T

Brake operation test

	Left hand	Right hand
Brake engine stroke	270 mm	270 mm
Length of initial quick-drip (Emergency)	148 mm	130 mm
Full load torque position	Nil mm	Nil mm
Fast Braking time (90% stroke)	1.2 sec	1.3 sec
Slow braking time (90% stroke)	5.0 sec	5.9 sec
Conversion to fast braking (midshaft)	N/C m/s	N/C m/s
Conversion to fast braking (end-of-wind) (top)	N/C TN/C T	N/C TN/C T
	(bottom)	N/C TN/C T

Brake holding test against power: (tested with max. out of balance rope plus 1,5 x rated motor torque (geared winders).

2,5 x rated motor torque (direct coupled winders).

Left Hand 3 000 A movement Nil Right Hand 3000 A movement Nil

Trigger level (Escort braking system) LH m/S<sup>2</sup> rh m/S<sup>2</sup> ( m/S<sup>2</sup>)

Overspeed protection: Type Lilly Duplex Left Hand Right Hand

Overspeed alarm contact float 0,0 mm 0,2 mm

Overspeed alarm contact gap with roller on top of cam 1,0 mm 0,5 mm

Minimum trip speed (with roller on top of cam)  
 (top) N/C m/s N/C m/s  
 (bottom) 2,0m/s 1,3 m/s

Overspeed alarm contact gap at full speed 1,0 mm 0,3 mm  
 Deceleration cam position Correct Correct